

# Can a TAG Semantics Be Compositional?

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Stanford, California 94305, USA.*



# Outline

Review of synchronous TAG for semantics

What compositionality is and isn't

- What it ought to mean to be worth worrying about
- Why it is a subjective notion

Relation to bimorphisms

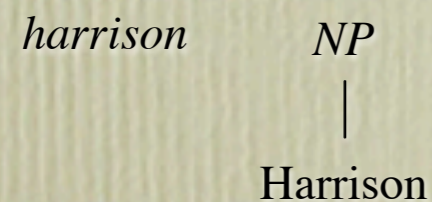
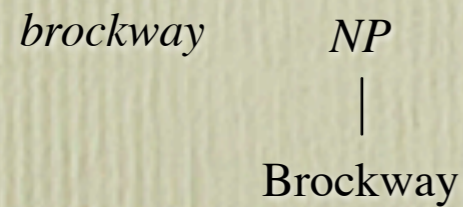
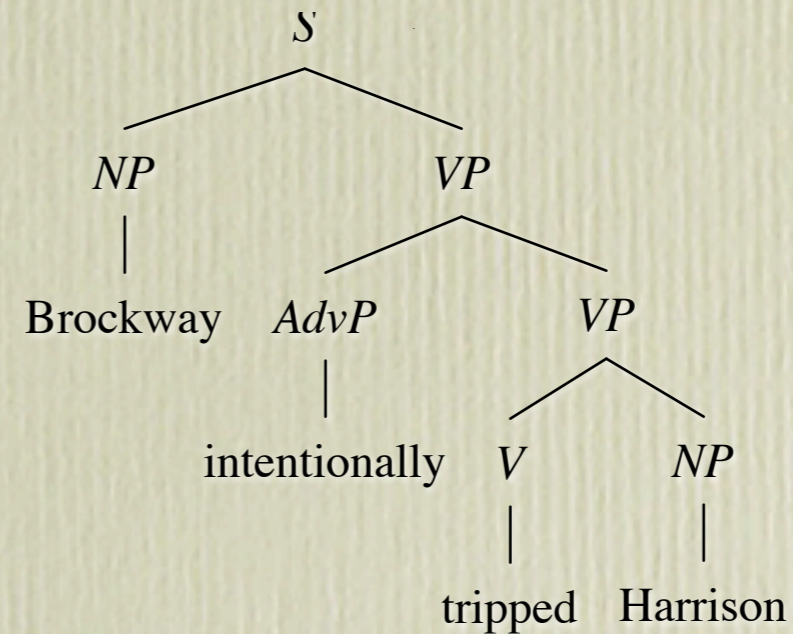
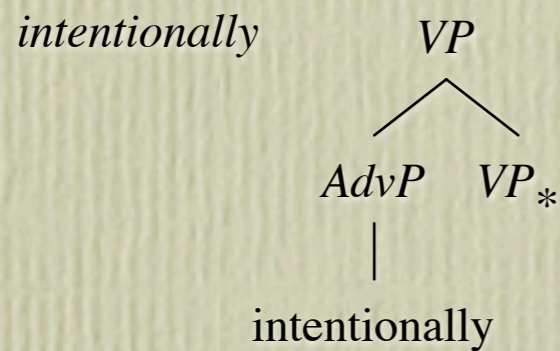
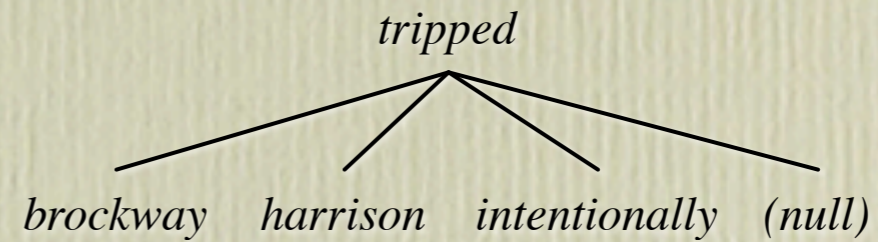
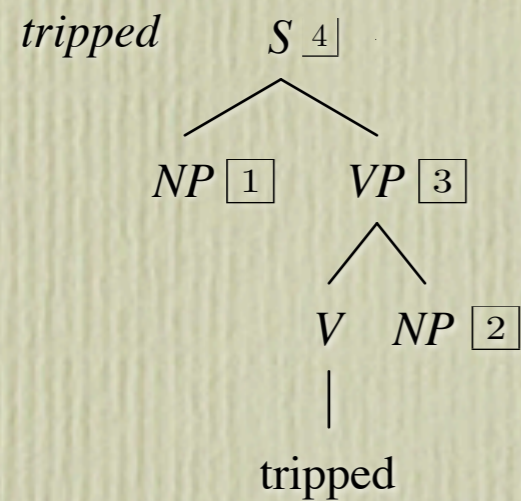
Where synchronous TAG semantics are and aren't  
compositional



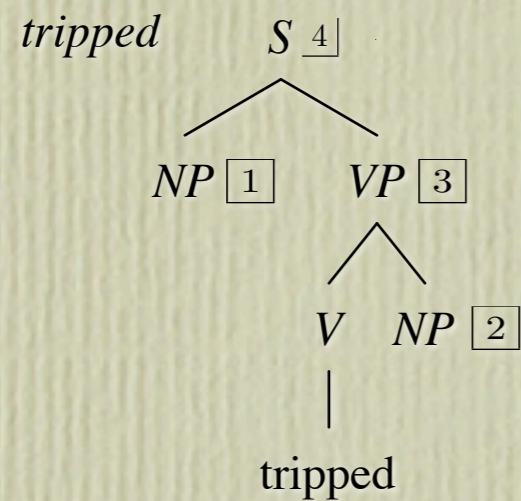
# Synchronous TAG Semantics



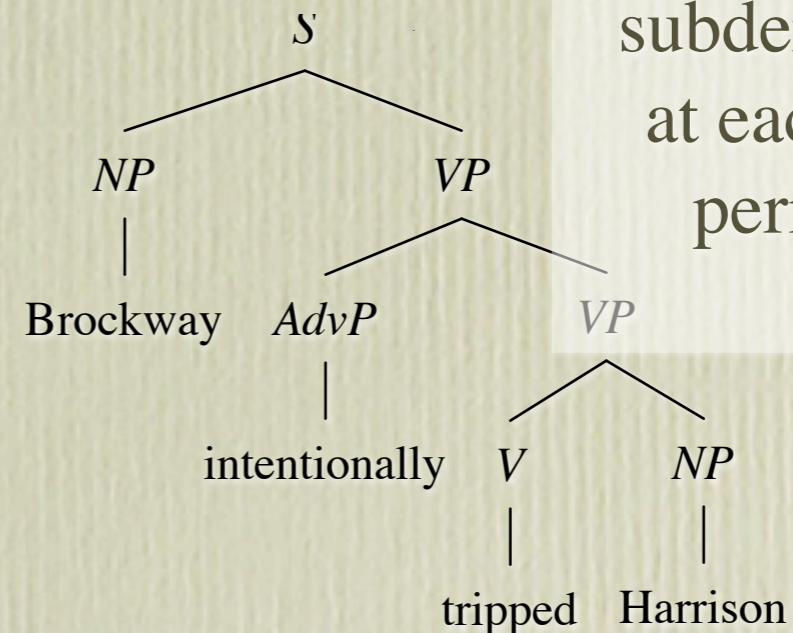
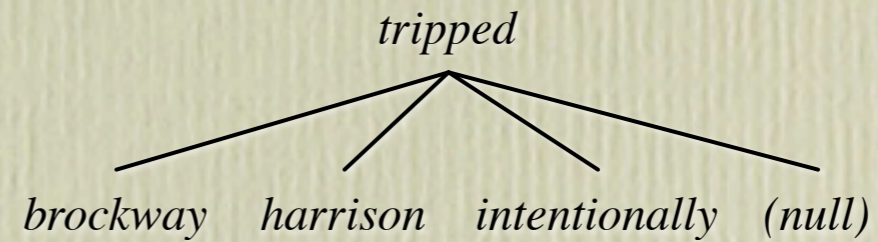
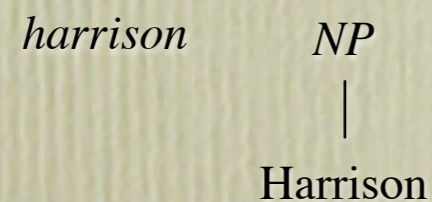
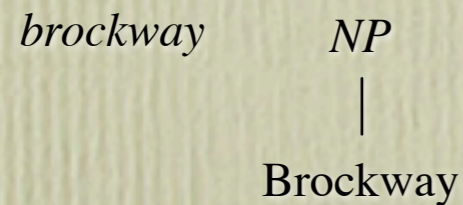
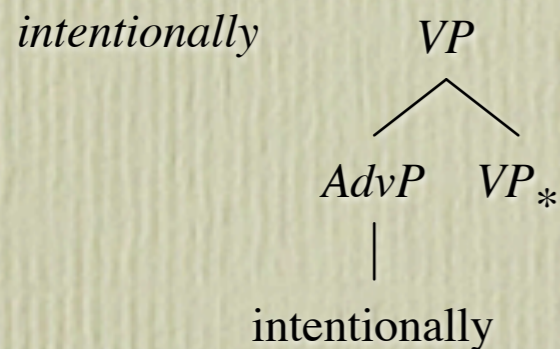
# TAG Syntax



# TAG Syntax



Numbered  
“links” mark  
and provide a  
permutation of  
adjunction and  
substitution  
sites

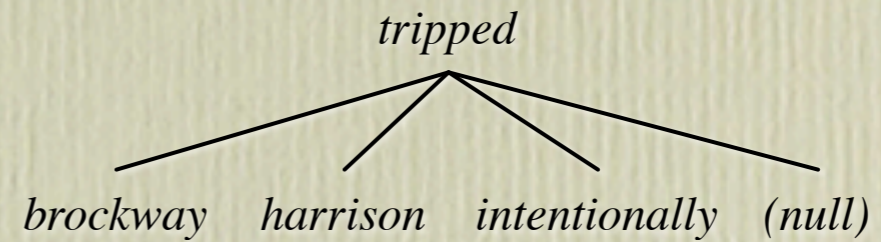
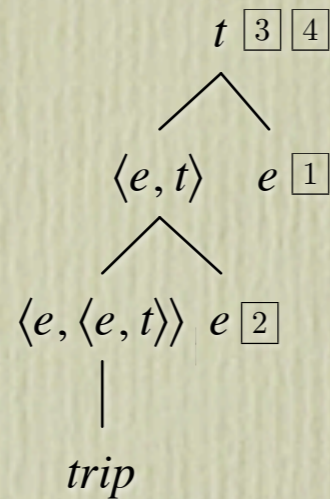


Derivation tree  
specifies  
subderivations  
at each site in  
permutation  
order.

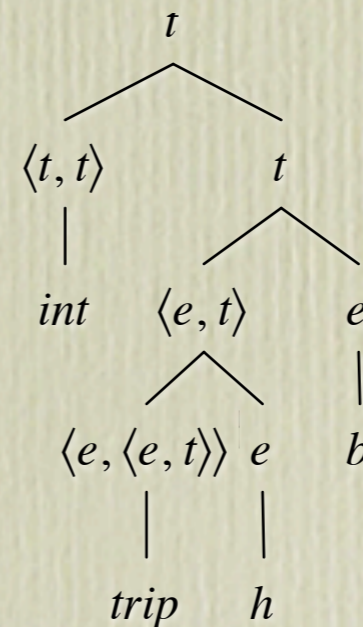
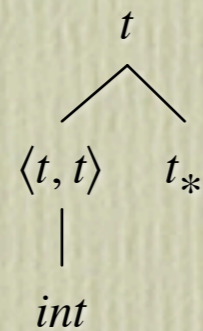


# TAG Semantics

*tripped*



*intentionally*



*brockway*

*e*  
|  
*b*

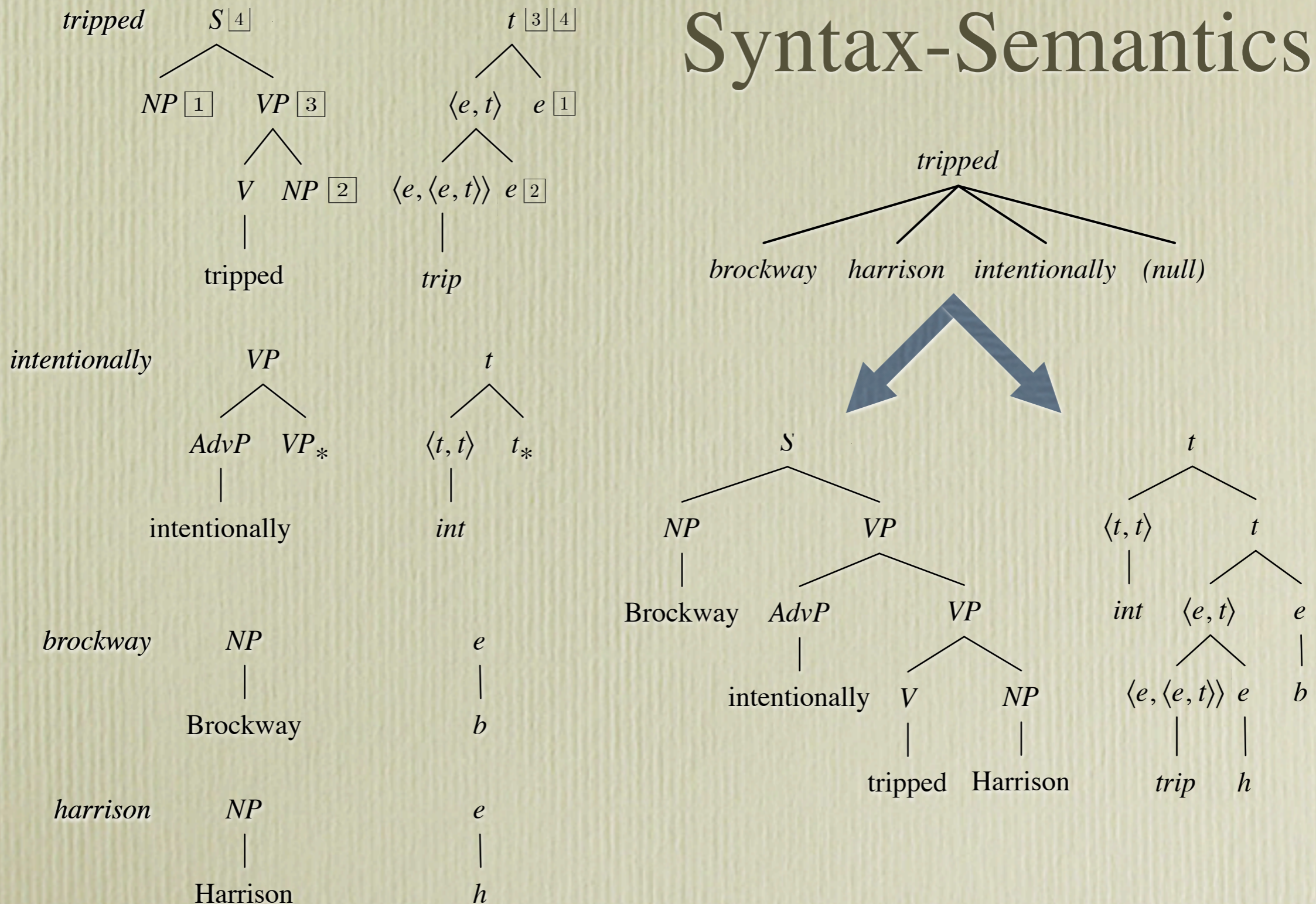
*harrison*

*e*  
|  
*h*



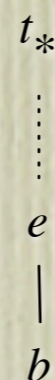
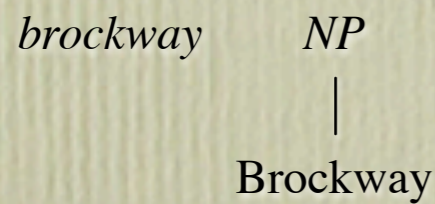
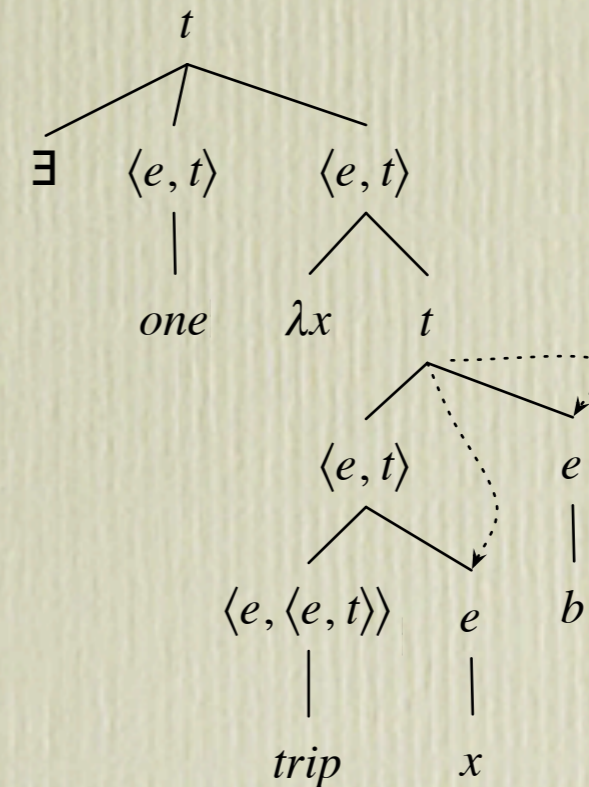
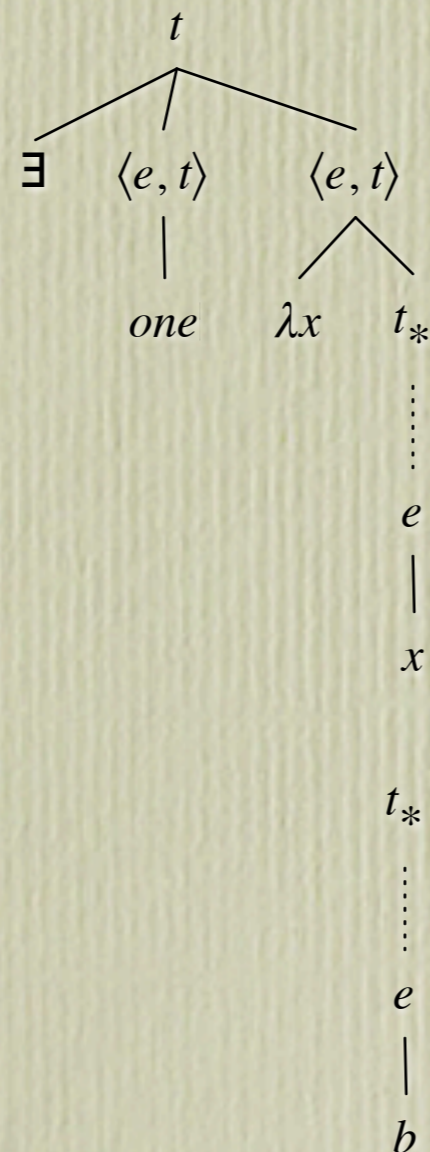
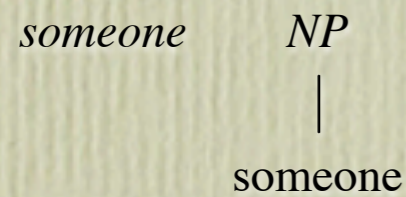
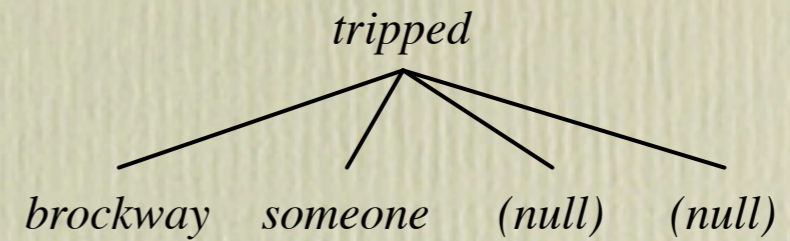
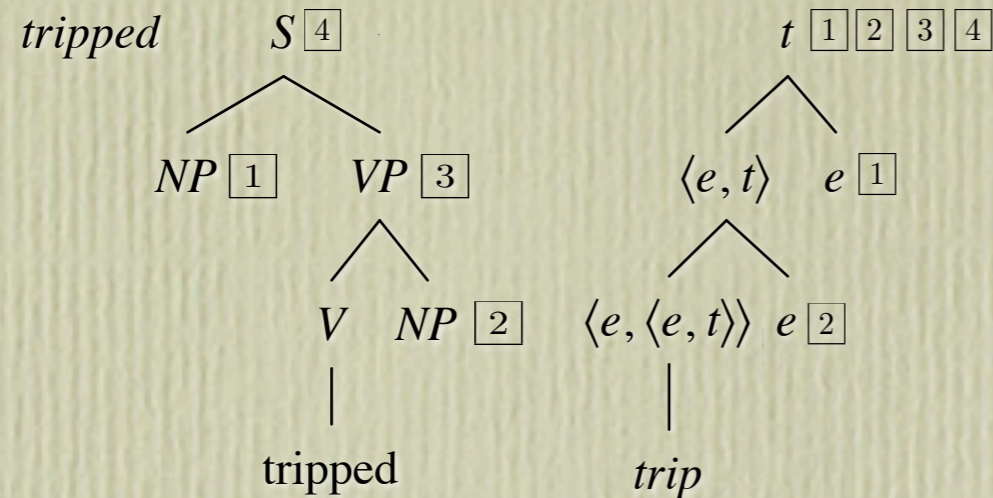
# Synchronous TAG

## Syntax-Semantics





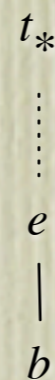
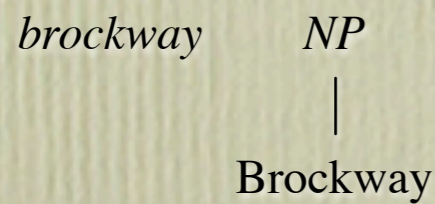
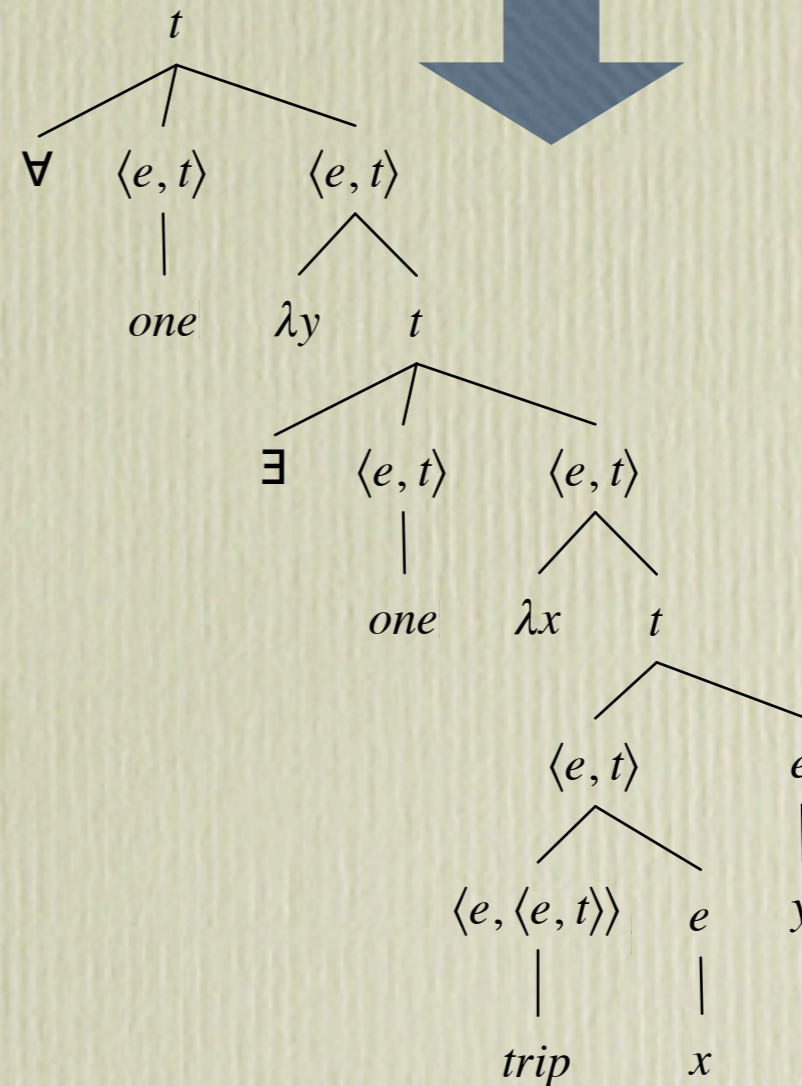
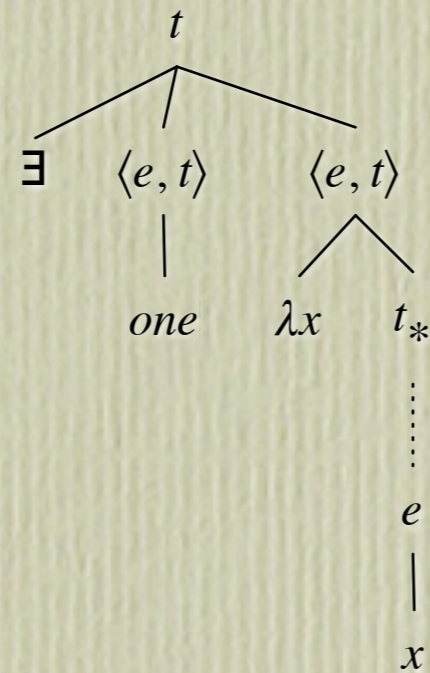
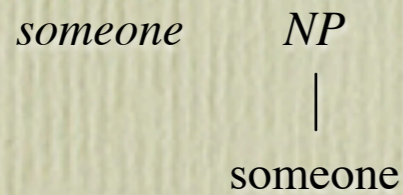
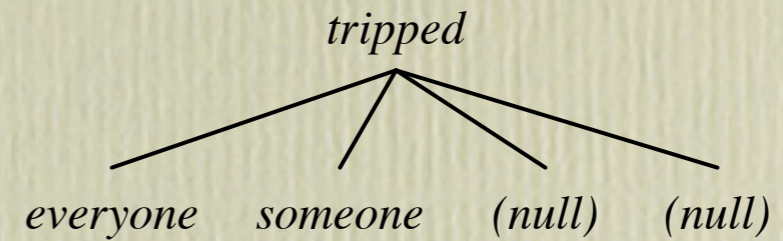
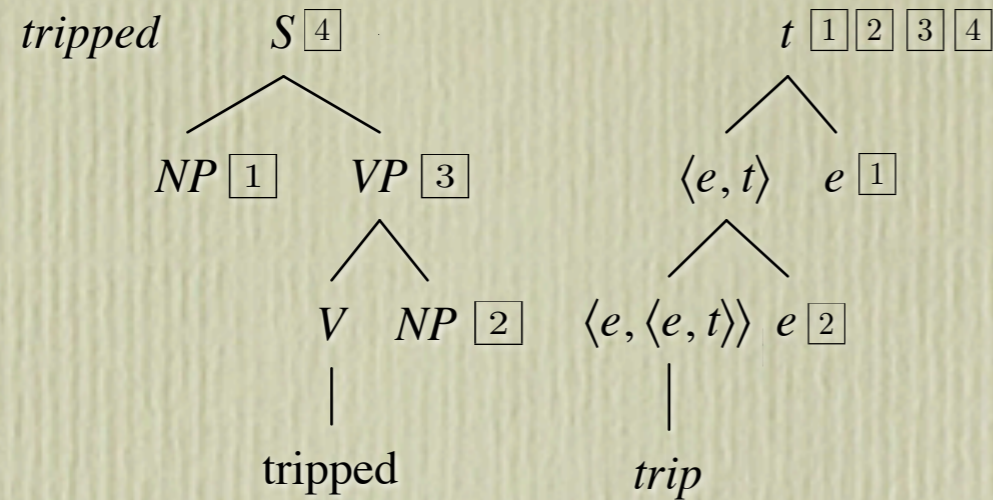
# Quantifiers



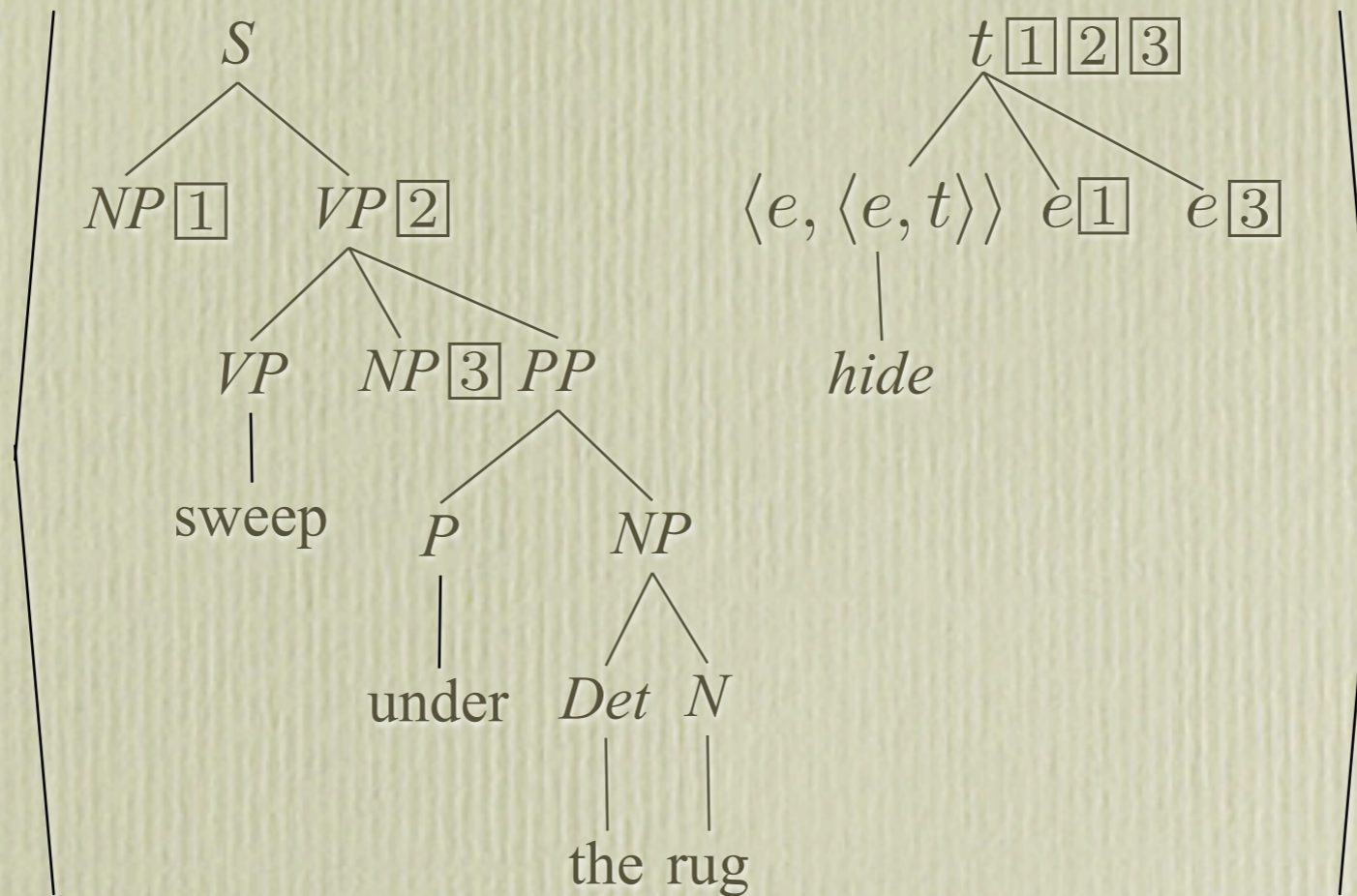
$$\exists(\text{one}, \lambda x.\text{trip}(b, x))$$



# Quantifiers



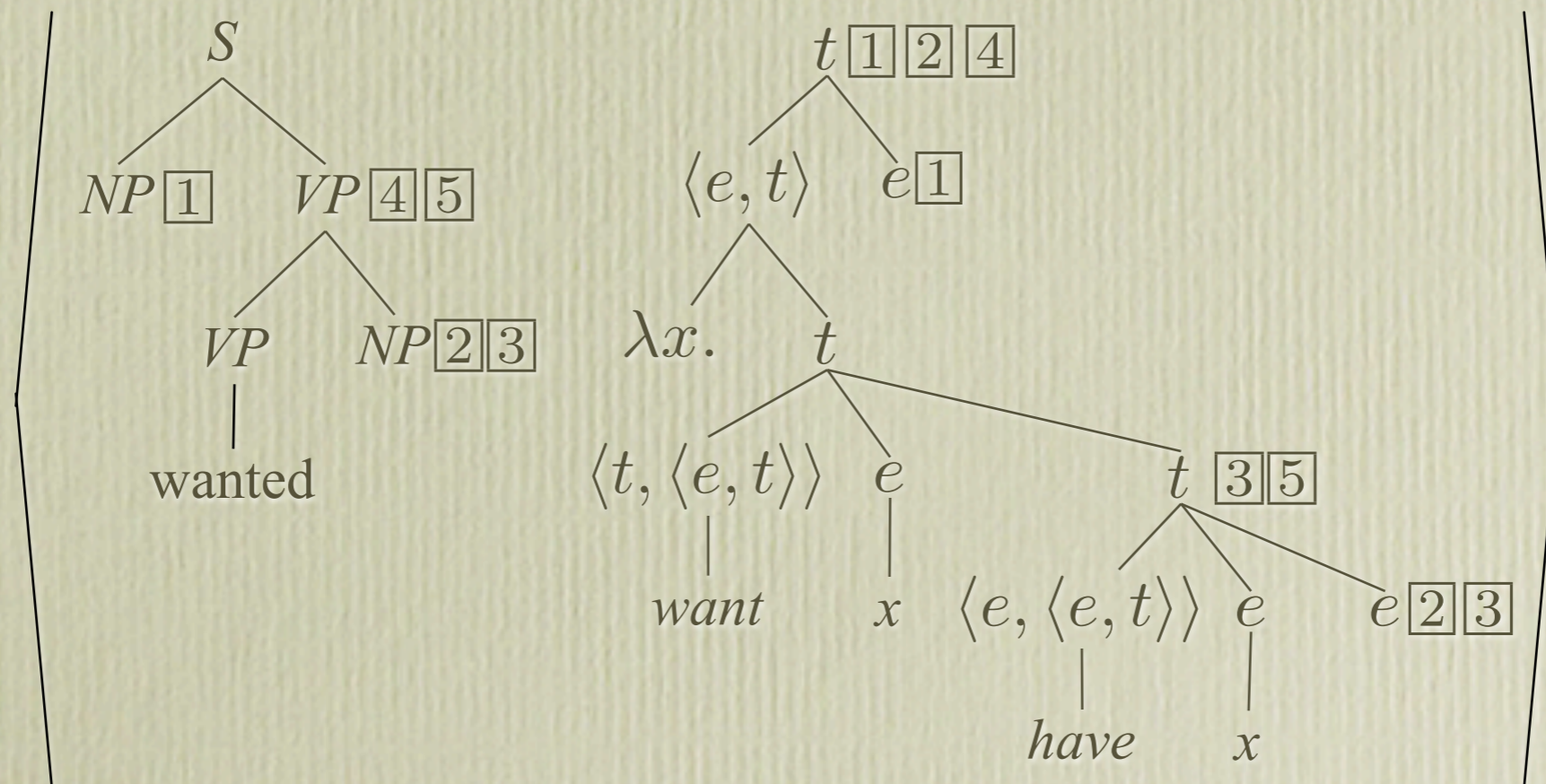
# Complex Syntax with Simple Semantics: Idioms



# Simple Syntax with Complex Semantics: Semantic Decomposition

Kim wanted the report tomorrow.

- $want(k, tomorrow(have(k, the-report)))$   
 $= [\lambda x.want(x, tomorrow(have(x, the-report)))]k$



— McCawley, 1979, pages 84-86

# Coverage

Can handle several putatively hard cases without additional machinery (with reservations...):

- Scope ambiguities  
*Everyone loves someone.*
- Scope interactions of VP-modifiers and quantifiers  
*Sandy usually likes everyone.*
- No scope out of finite clause  
*Sandy thinks everyone loves someone.*
- Pied-piped relative clauses  
*A problem whose solution was difficult stumped Bill.*
- Embedded quantifiers in prepositional phrases  
*Two politicians spy on someone from every city.*

— Kallmeyer, Romero, Joshi



# Compositionality



# Compositionality

*A means for guaranteeing the systematicity of the syntax-semantics relation.*

**Compositionality (informal):** The meaning of an expression is determined by the meanings of its immediate parts along with their method of combination.

“The meaning of a compound expression is a function of the meaning of its parts and of the syntactic rule by which they are combined.” (Partee et al., 1990, p. 318, as cited by Janssen, 1997)



# A Compositional Semantics

$Num \rightarrow Num\ Digit$

$Num \rightarrow Digit$

$Digit \rightarrow \underline{0}$

$Digit \rightarrow \underline{1}$





# A Compositional Semantics

$$\begin{array}{llll} \textit{Num} & \rightarrow & \textit{Num Digit} & 10 \times \llbracket \textit{Num} \rrbracket + \llbracket \textit{Digit} \rrbracket \\ \textit{Num} & \rightarrow & \textit{Digit} & \llbracket \textit{Digit} \rrbracket \\ \textit{Digit} & \rightarrow & \underline{0} & 0 \\ \textit{Digit} & \rightarrow & \underline{1} & 1 \end{array}$$



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$$\begin{aligned} \llbracket \underline{101} \rrbracket &= 10 \times \llbracket \underline{10} \rrbracket + \llbracket \underline{1} \rrbracket \\ &= 10 \times (10 \times \llbracket \underline{1} \rrbracket + \llbracket \underline{0} \rrbracket) + \llbracket \underline{1} \rrbracket \\ &= 10 \times (10 \times 1 + 0) + 1 \\ &= 101 \text{ (5)} \end{aligned}$$

$$\llbracket \underline{0011} \rrbracket = 3$$



# Near Misses

**Precompositionality:** The meaning of an expression is determined by its parts.

**Representational compositionality:** The meaning representation of an expression is determined by the meaning representations of its parts along with their method of combination.



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$$\begin{array}{l} A \rightarrow BC \quad [A \ [B] \ [C]] \\ S^* \rightarrow S \quad \mu([S]) \end{array}$$

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**Representational compositionality:** The meaning representation of an expression is determined by the meaning representations of its parts along with their method of combination.



# Montague's Approach

**Montagovian compositionality:** The meaning of an expression is a homomorphic image of the expression's syntactic derivation.

$$h(\text{OP}(P, Q)) = \hat{h}_{\text{OP}}(h(P), h(Q))$$

$$[[Num\ Digit]] = 10 \times [[Num]] + [[Digit]]$$

$$\hat{h} = \lambda x, y. 10 \times x + y$$



# An Example: Relative Clauses

- S3:** If  $\zeta \in P_{CN}$  and  $\phi \in P_t$ , then  $F_{3,n}(\zeta, \phi) = \zeta$  **such that**  $\phi'$ , and  $\phi'$  comes from  $\phi$  by replacing each occurrence of  $he_n$  or  $him_n$  by [the gender-appropriate unsubscripted pronoun].
- T3:** If  $\zeta \in P_{CN}$ ,  $\phi \in P_t$ , and  $\zeta, \phi$  translate into  $\zeta', \phi'$  respectively, then  $F_{3,n}(\zeta, \phi)$  translates into  $\lambda x_n. \zeta'(x_n) \wedge \phi'$ .

(Montague, 1970, PTQ)



# Dispensibility of Logical Form

**Montague's relative clause translation rule:** “If  $\zeta \in P_{CN}$ ,  $\phi \in P_t$ , and  $\zeta, \phi$  translate into  $\zeta', \phi'$  respectively, then  $F_{3,n}(\zeta, \phi)$  translates into  $\lambda x_n. \zeta'(x_n) \wedge \phi'$ .”

**Thomason's clarificatory footnote:** “To avoid collision of variables, the translation must be  $\lambda x_m. \zeta(x_m) \wedge \psi$ , where  $\psi$  is the result of replacing all occurrences of  $x_n$  in  $\phi'$  by occurrences of  $x_m$ , where  $m$  is the least even number such that  $x_m$  has no occurrences in either  $\zeta'$  or  $\phi'$ .”

**Janssen's correction:** “Thomason's reformulation is an operation on representations, and not on meanings. . . . The operation on meanings can be represented in a much simpler way, using a polynomial, viz.:

$$[\lambda P. (\lambda x_n. P(x_n) \wedge \phi')](\zeta') \quad ”$$





# An Example: Relative Clauses

**S3:** If  $\zeta \in P_{CN}$  and  $\phi \in P_t$ , then  $F_{3,n}(\zeta, \phi) = \zeta$  **such that**  $\phi'$ , and  $\phi'$  comes from  $\phi$  by replacing each occurrence of  $he_n$  or  $him_n$  by [the gender-appropriate unsubscripted pronoun].

**T3:** If  $\zeta \in P_{CN}$ ,  $\phi \in P_t$ , and  $\zeta, \phi$  translate into  $\zeta', \phi'$  respectively, then  $F_{3,n}(\zeta, \phi)$  translates into  $\lambda x_n. \zeta'(x_n) \wedge \phi'$ .

“man such that he left”

- “man” • “such that he<sub>2</sub> left”
- $man \bullet left(x_2)$
- $\lambda x_2. man(x_2) \wedge left(x_2)$
- $[\lambda P. (\lambda x_2. P(x_2) \wedge left(x_2))](man)$



# Is Compositionality Possible?

$Num \rightarrow Num\ Digit$

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# Is Compositionality Possible?

$$\begin{array}{ll} \textit{Num} \rightarrow \textit{Num Digit} & \textit{Num} \rightarrow \textit{Digit Num} \\ \textit{Num} \rightarrow \textit{Digit} & \textit{Num} \rightarrow \textit{Digit} \\ \textit{Digit} \rightarrow \underline{0} & \textit{Digit} \rightarrow \underline{0} \\ \textit{Digit} \rightarrow \underline{1} & \textit{Digit} \rightarrow \underline{1} \end{array}$$

Impossibility of compositional semantics for this language:

$$\begin{aligned} \llbracket \underline{101} \rrbracket &= f(\llbracket \underline{1} \rrbracket, \llbracket \underline{01} \rrbracket) \\ &= f(\llbracket \underline{1} \rrbracket, \llbracket \underline{1} \rrbracket) \\ &= \llbracket \underline{11} \rrbracket \end{aligned}$$



# Is Compositionality Vacuous?

For arbitrary language  $L$  and meaning function  $[[\cdot]] : L \rightarrow M$ , there is a function  $\mu : L \rightarrow M'$  such that

$$\begin{aligned}\mu(P \ Q) &= \mu(P)(\mu(Q)) \\ \mu(P \ \neg) &= [[P]]\end{aligned}$$

(Zadrozny, 1994)



# The Counterexample Revisited

$Num \rightarrow Num\ Digit$	$Num \rightarrow Digit\ Num$
$Num \rightarrow Digit$	$Num \rightarrow Digit$
$Digit \rightarrow \underline{0}$	$Digit \rightarrow \underline{0}$
$Digit \rightarrow \underline{1}$	$Digit \rightarrow \underline{1}$

$Num \rightarrow Digit\ Num$	$\langle 10^{\llbracket Num \rrbracket_2} \times \llbracket Digit \rrbracket_1 + \llbracket Num \rrbracket_1, \llbracket Digit \rrbracket_2 + \llbracket Num \rrbracket_2 \rangle$
$Num \rightarrow Digit$	$\llbracket Digit \rrbracket$
$Digit \rightarrow \underline{0}$	$\langle 0, 1 \rangle$
$Digit \rightarrow \underline{1}$	$\langle 1, 1 \rangle$
$S \rightarrow Num \dashv$	$\llbracket Num \rrbracket_1$



# Montague's Approach

**Montagovian compositionality:** The meaning of an expression is a homomorphic image of the expression's syntactic derivation.

Contextual non-synonymy:

- I believe Lewis Carroll is the greatest children's book author.
- I believe Charles Dodgson is the greatest children's book author.



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*Adjust denotations:  $e \Rightarrow \langle s, e \rangle$*



# Subjectivity of Compositionality

**Compositionality (informal):** The meaning of an expression is determined by the meanings of its immediate parts along with their method of combination.

- What are appropriate meanings?
  - $[[\underline{101}]] = 5$   
 $[[10\underline{1}]] = \langle 5, 3 \rangle$   
 $[[\underline{1}0\underline{1}]] = [ \underline{1} [ \underline{0} [ \underline{1} ] ] ]$
  - $[[\text{Lewis Carroll}]] : e$   
 $[[\text{Lewis Carroll}]] : \langle s, e \rangle$





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- $[[\underline{101}]] = 5$

- ~~•  $[[\underline{101}]] = \langle 5, 3 \rangle$~~

- ~~•  $[[\underline{101}]] = [ \underline{1} [ \underline{0} [ \underline{1} ] ] ]$~~

- $[[\text{Lewis Carroll}]] : e$

- $[[\text{Lewis Carroll}]] : \langle s, e \rangle$



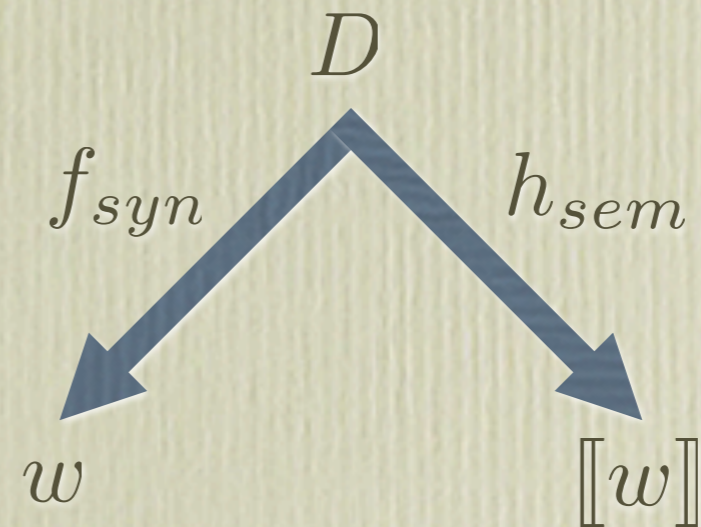
# Compositionality of STAG Semantics



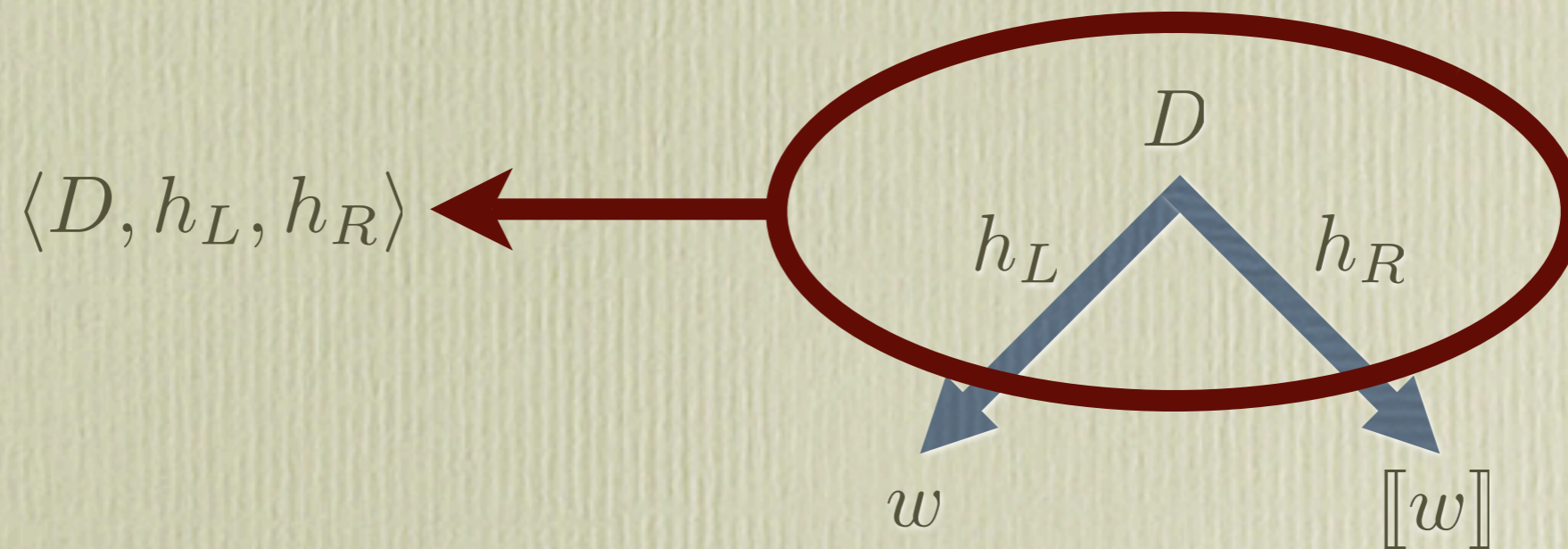
# Compositionality

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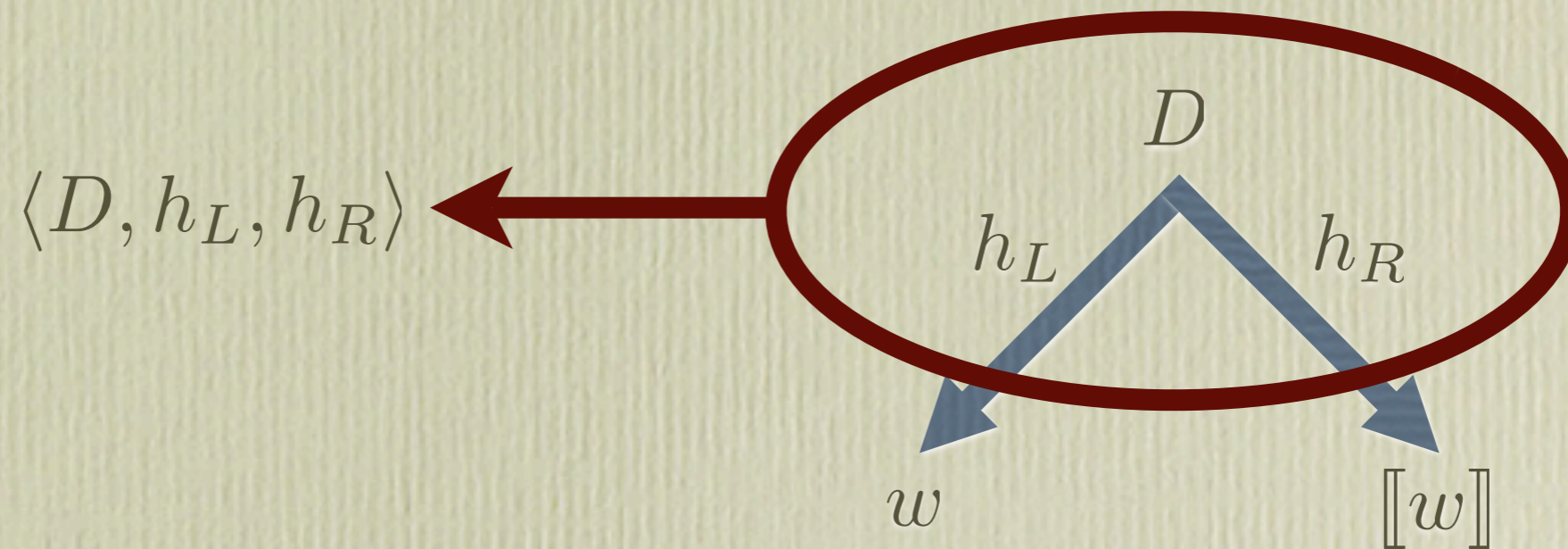
$$\begin{aligned}w &= f_{syn}(D) \\ [[w]] &= h_{sem}(D)\end{aligned}$$



# Compositionality and Bimorphisms



# Compositionality and Bimorphisms



$B(L, R)$

---

$B(D, M)$	tree transduction
$B(LC, LC)$	STSG
$B(ELC, ELC)$	STAG
$B(arb, M)$	compositional relation

# Summary

Compositional relation defined by

- A generalized bimorphism
  - Input function is arbitrary
  - Output function is a homomorphism
    - to a pretheoretically appropriate domain

$B(L, R)$

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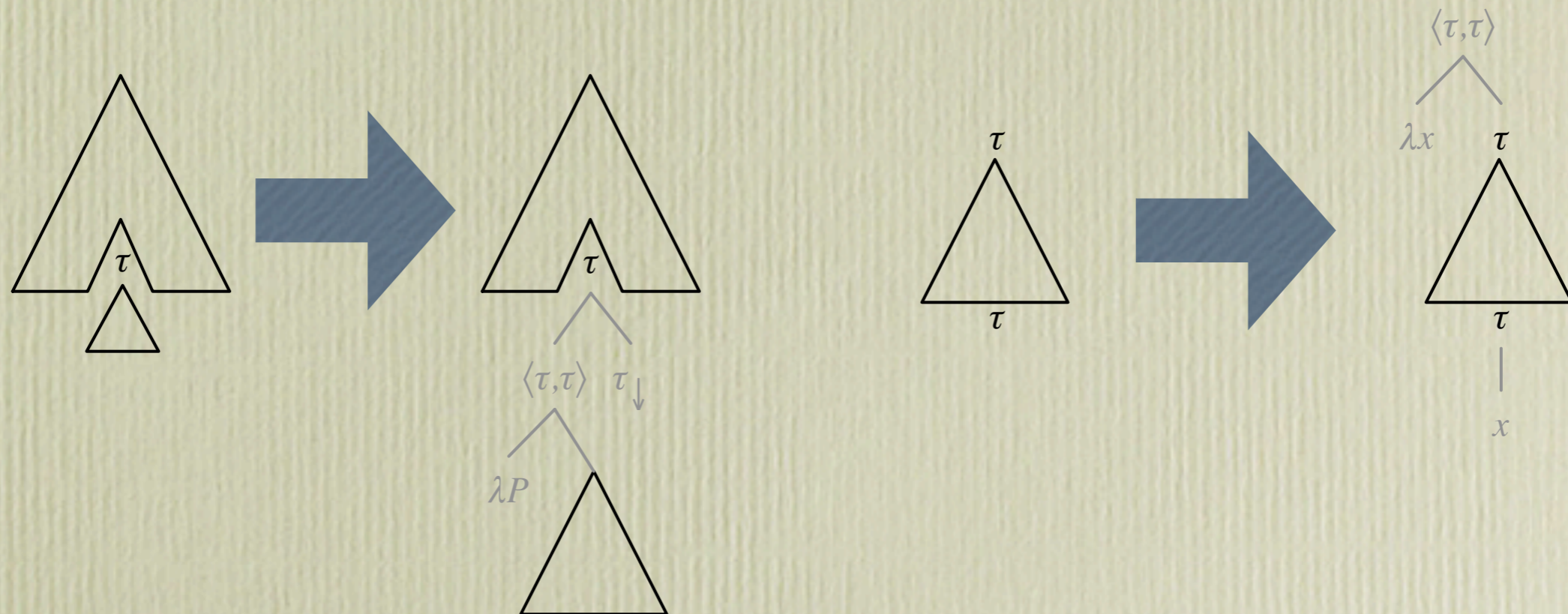
$B(LC, LC)$       STSG

~~$B(ELC, ELC)$       STAG~~

$B(arb, M)$       compositional relation

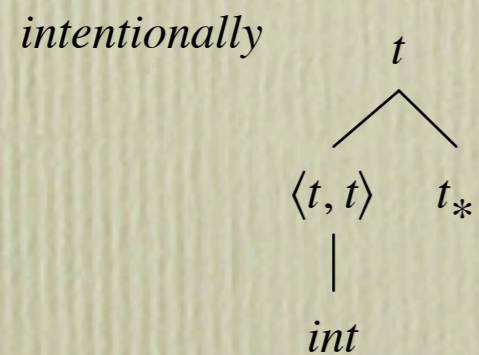
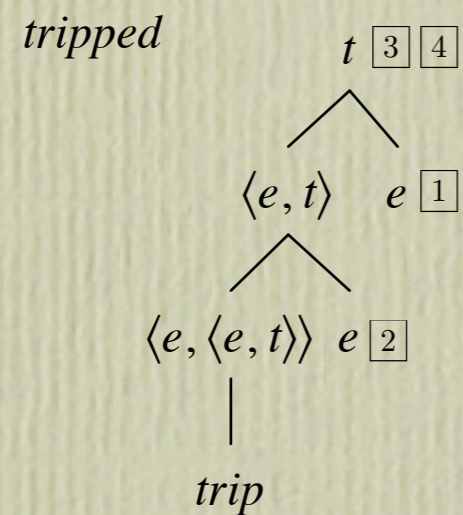


# TAG to TSG

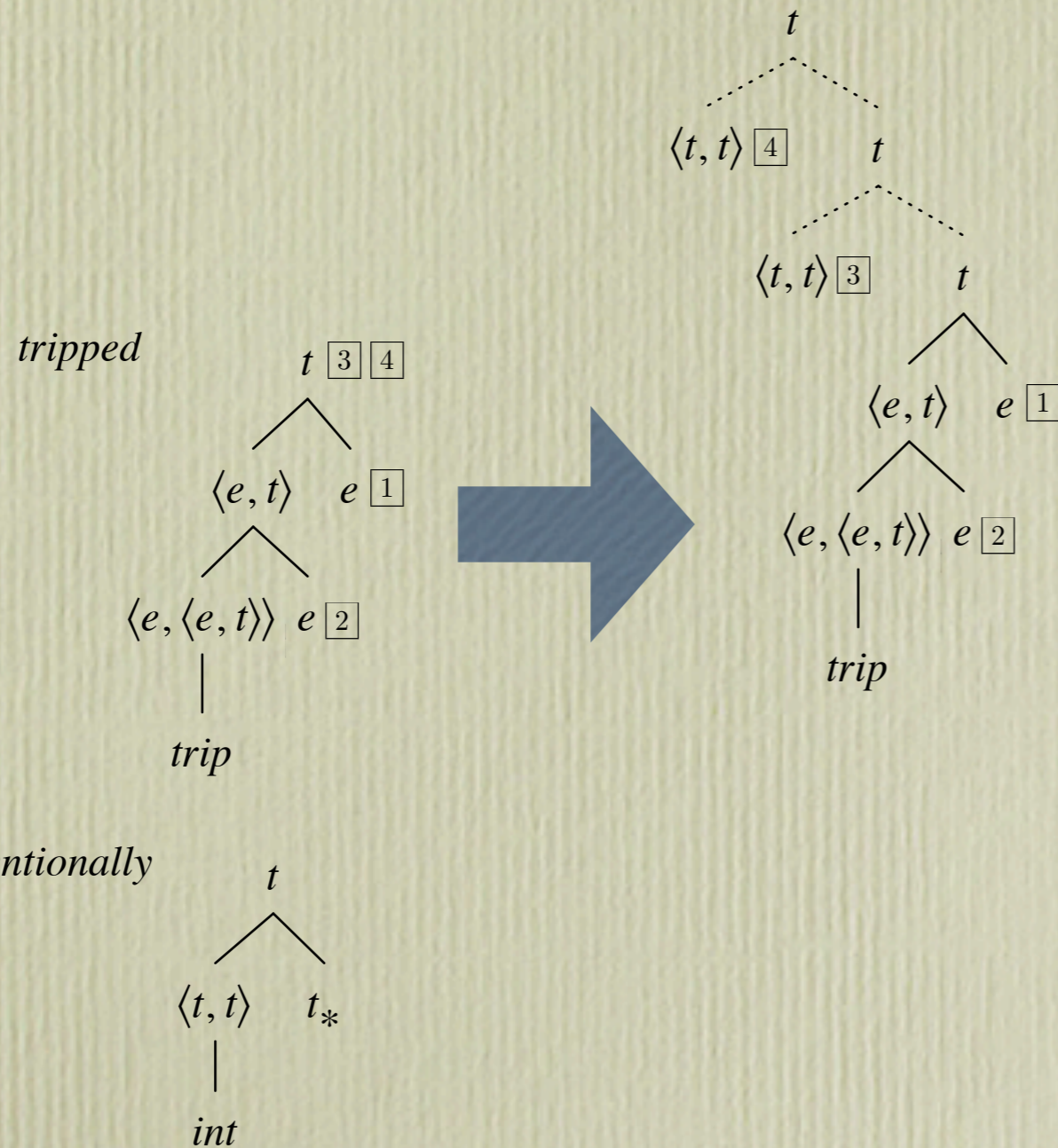




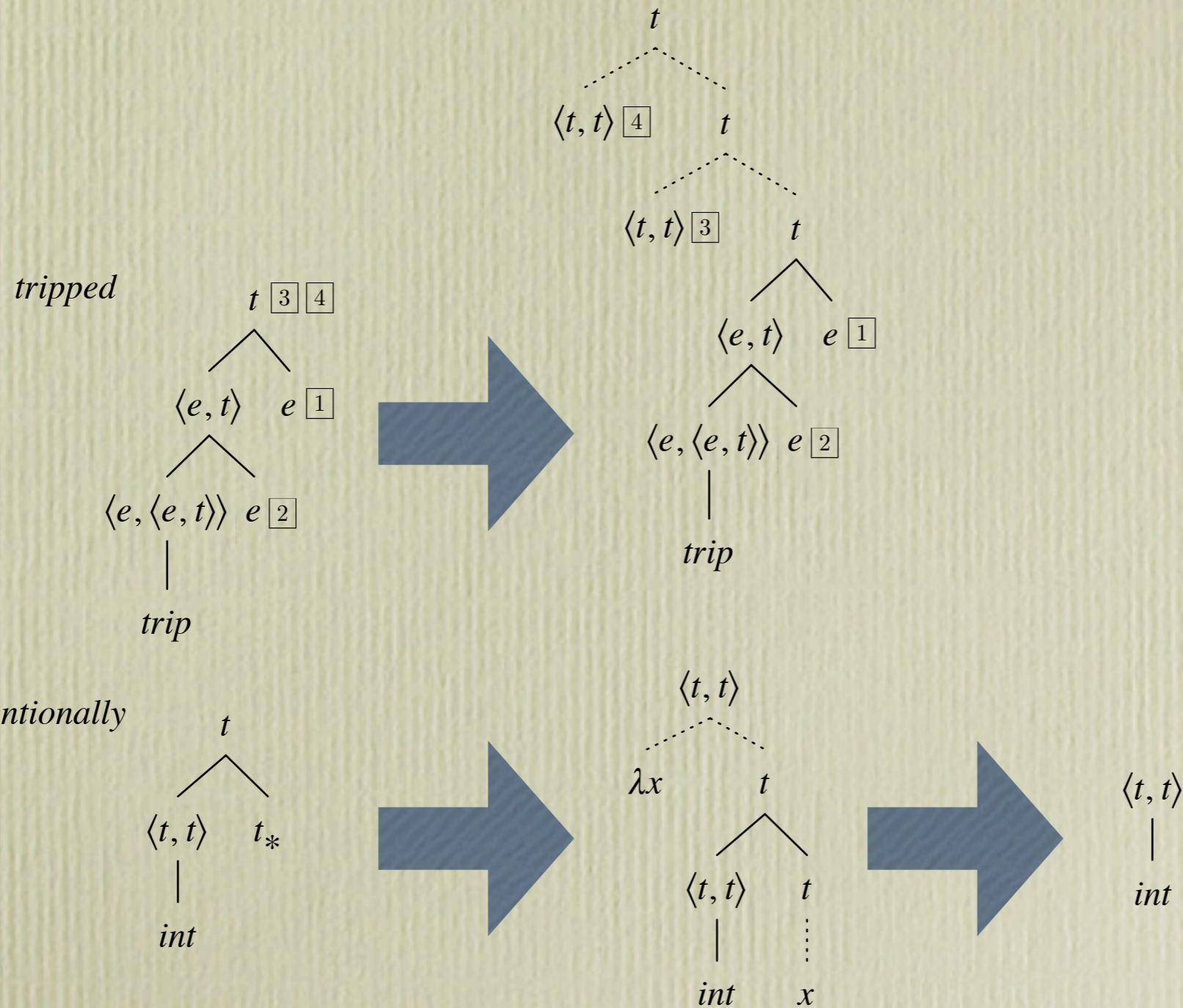
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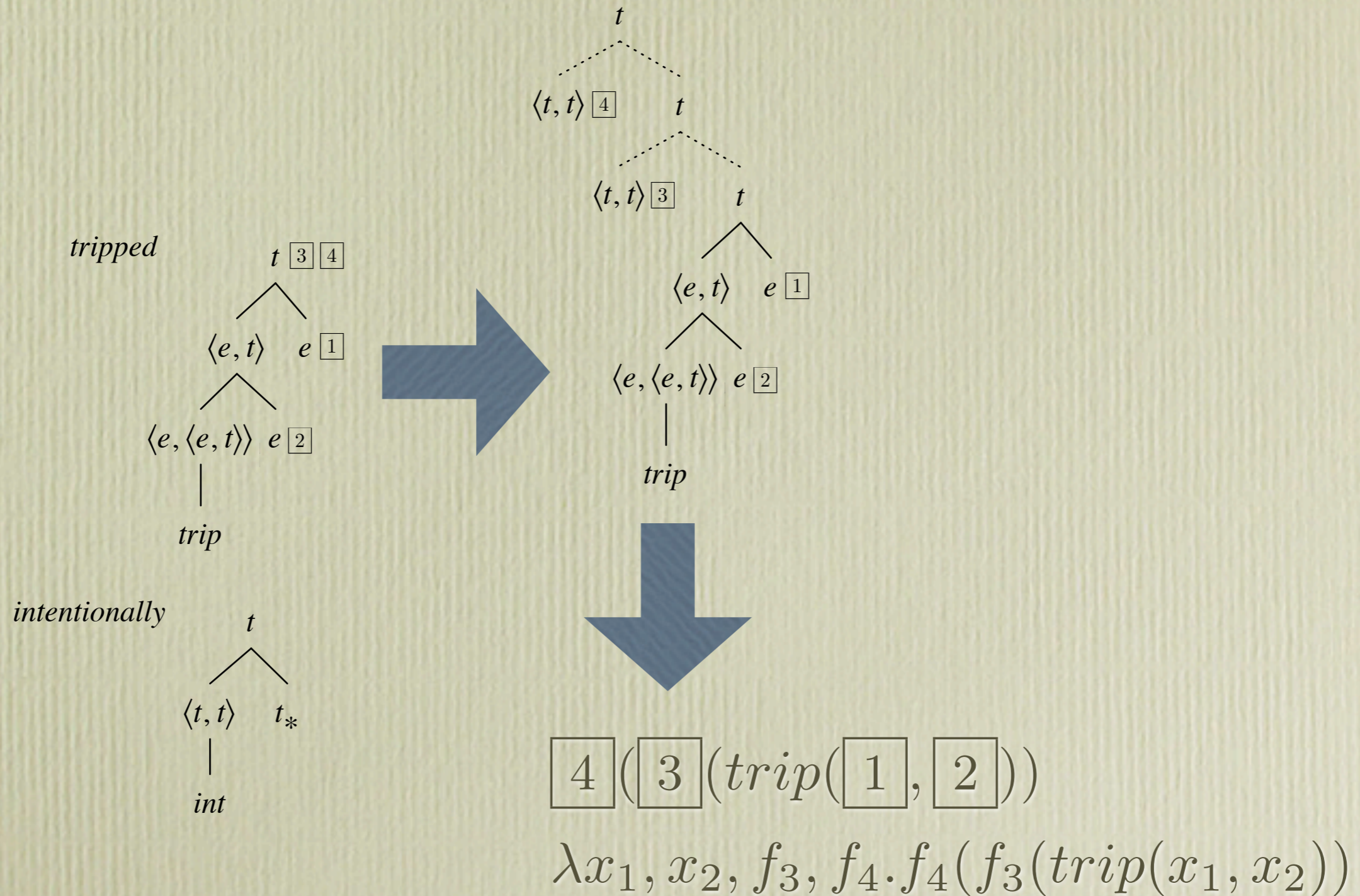
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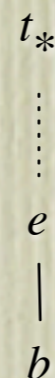
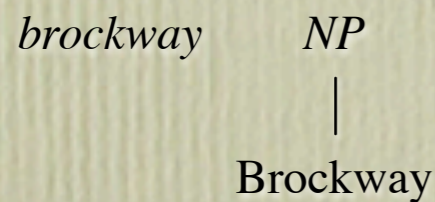
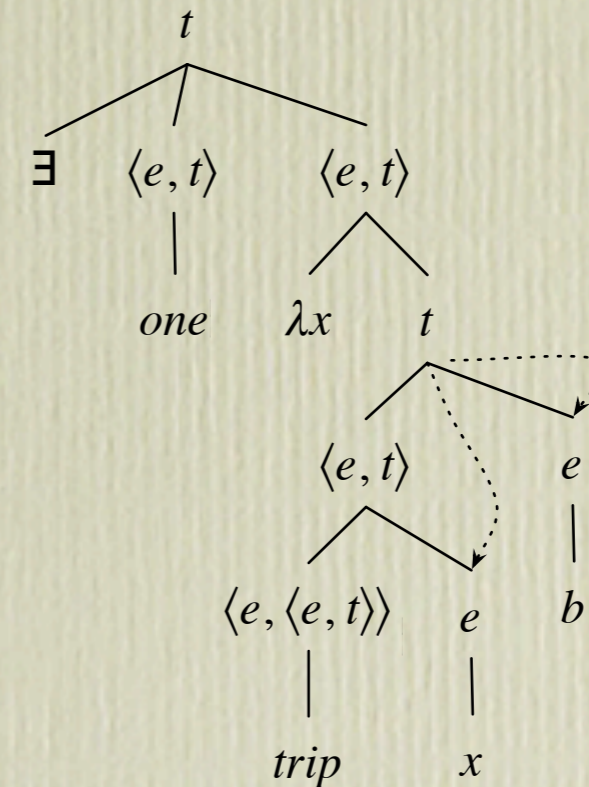
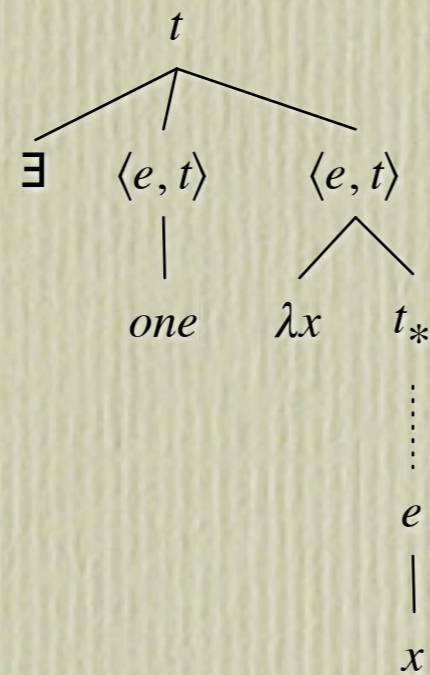
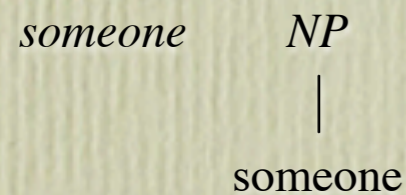
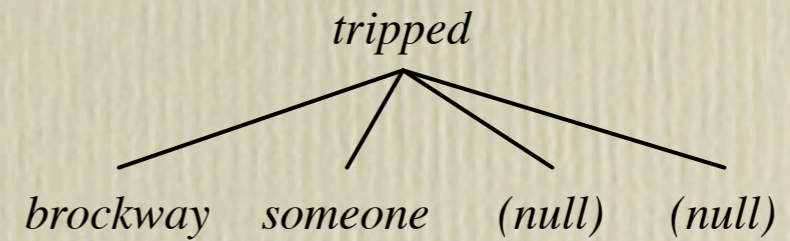
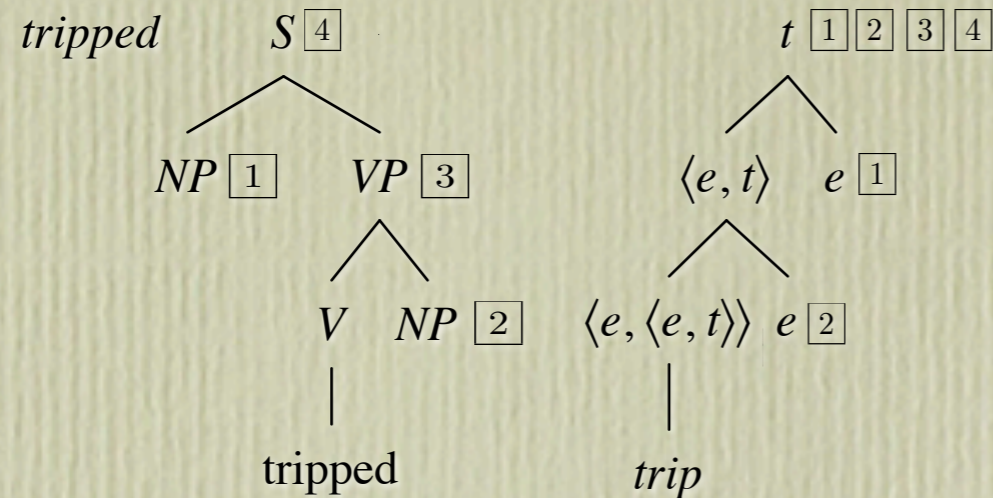
# TAG to TSG



# TAG to TSG



# Quantifiers



$$\exists(\text{one}, \lambda x.\text{trip}(b, x))$$



# Compositional STAG

## Quantifier Analyses

1. Reconstruct open meaning representations as self-contained semantic objects
2. Use an analysis with closed representations
  - “Variable-free semantics”
  - Hendriks, 1993



# Conclusion

Why compositionality?

- Pelletier: “Warm, fuzzy feeling”
- Janssen: As a guide for restrictive theorizing
- As a means for guaranteeing systematicity

Is STAG semantics compositional?

- More than you would have thought
- Less than completely

